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# PRIVACY-PRESERVING DATA MINING: MODELS AND ALGORITHMS





# PRIVACY-PRESERVING DATA MINING: MODELS AND ALGORITHMS

Edited by

**CHARU C. AGGARWAL**

IBM T. J. Watson Research Center, Hawthorne, NY 10532

**PHILIP S. YU**

University of Illinois at Chicago, Chicago, IL 60607

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